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| **Recommendation ITU-R F.1245-2**  **(03/2012)** |
| **Mathematical model of average and related radiation patterns for line-of-sight  point-to-point fixed wireless system antennas for use in certain coodination studies and interference assessment in  the frequency range from  1 GHz to about 70 GHz** |
| **F Series**  **Fixed service** |

Foreword

The role of the Radiocommunication Sector is to ensure the rational, equitable, efficient and economical use of the radio-frequency spectrum by all radiocommunication services, including satellite services, and carry out studies without limit of frequency range on the basis of which Recommendations are adopted.

The regulatory and policy functions of the Radiocommunication Sector are performed by World and Regional Radiocommunication Conferences and Radiocommunication Assemblies supported by Study Groups.

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| **TF** | Time signals and frequency standards emissions |
| **V** | Vocabulary and related subjects |

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| ***Note***: *This ITU-R Recommendation was approved in English under the procedure detailed in Resolution ITU-R 1.* |

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RECOMMENDATION ITU-R F.1245‑2[[1]](#footnote-1)\*

Mathematical model of average and related radiation patterns for   
line-of-sight point-to-point fixed wireless system antennas for use in   
certain coordination studies and interference assessment in the   
frequency range from 1 GHz to about 70 GHz

(Question ITU-R 110-2/5)

(1997-2000-2012)

Scope

This Recommendation provides average and related reference radiation patterns for line-of-sight point-to-point fixed wireless system (FWS) antennas in the frequency range from 1 GHz to about 70 GHz. The analysis in this Recommendation may be used in certain coordination studies and interference assessments when particular information concerning the FWS antenna is not available.

The ITU Radiocommunication Assembly,

considering

a) that the reference radiation pattern of line-of-sight point-to-point fixed wireless system (FWS) antennas stated in Recommendation ITU-R F.699 gives the peak envelope of side‑lobe patterns;

b) that if the peak envelope radiation pattern is used in the assessment of the aggregate interference consisting of many interference entries, the predicted interference will result in values that are greater than values that would be experienced in practice;

c) that, therefore, it is necessary to use the antenna radiation pattern representing average side-lobe levels in the following cases:

– to predict the aggregate interference to a geostationary or non-geostationary satellite from numerous radio-relay stations;

– to predict the aggregate interference to a radio-relay station from many geostationary satellites;

– to predict interference to a radio-relay station from one or more non-geostationary satellites under the continuously variable angle which should be averaged;

– in any other cases where the use of the radiation pattern representing average side-lobe levels is appropriate;

d) that a simple mathematical formula is preferable to the radiation pattern representing average side-lobe levels;

e) that a mathematical model is also required for generalized radiation patterns of antennas for statistical interference analyses involving a few interference entries such as from geostationary satellites into systems in the fixed service,

recommends

**1** that, in the absence of particular information concerning the radiation pattern of the line‑of-sight FWS antenna involved, the mathematical model of the average radiation pattern as stated below should be used for the applications referred to in *considering* c);

**2** that the following mathematical model of the average radiation pattern should be adopted for frequencies in the range 1-40 GHz and provisionally in the range 40 GHz to about 70 GHz;

**2.1** in cases where the ratio between the antenna diameter and the wavelength is greater than 100 (*D*/λ > 100), the following equation should be used (see Notes 1 and 7):

G(ϕ)  =  *Gmax*  –  2.5  ×  10–3  for 0º < ϕ < ϕ*m*

G(ϕ)  =  *G*1 for ϕ*m* ≤ ϕ < max (ϕ*m*, ϕ*r*)

G(ϕ)  =  29  –  25 log ϕ for max (ϕ*m*, ϕ*r*) ≤ ϕ< 48º

G(ϕ)  =  –13 for 48º ≤ ϕ ≤ 180º

where:

*Gmax*: maximum antenna gain (dBi) (see Note 2);

*G*(ϕ): gain (dBi) relative to an isotropic antenna;

ϕ: off-axis angle (degrees);

  expressed in the same unit;

*G*1: gain of the first side lobe;

 2  15 log (*D*/λ)

                  degrees

                  degrees

**2.2** in cases where the ratio between the antenna diameter and the wavelength is less than or equal to 100 (*D*/λ ≤ 100), the following equation should be used (see Notes 3 and 7):

*G*(ϕ)  =  *Gmax*  –  2.5  ×  10–3  for 0º <ϕ< ϕ*m*

*G*(ϕ)  =  39 – 5 log (*D*/λ)  –  25 log ϕ for ϕ*m* ≤ϕ< 48º

*G*(ϕ)  =  –3 – 5 log (*D*/λ) for 48º ≤ϕ≤ 180º

**3** that Annex 1 may be provisionally referred to for generalized radiation patterns of point-to-point FWS antennas which may be used only in statistical interference analyses involving a few interference entries such as from geostationary satellites into systems in the fixed service (see Note 9);

**4** that the following Notes should be regarded as part of this Recommendation.

NOTE 1 – The average side-lobe levels in § 2.1 are 3 dB lower than peak envelope side-lobe levels in § 2.1 of Recommendation ITU-R F.699.

NOTE 2 – The relationship between *Gmax* and *D*/λ is given in Recommendation ITU-R F.699.

NOTE 3 – The mathematical model in § 2.2 was derived from the condition that the total power emitted from the antenna should not exceed the total power fed into the antenna.

NOTE 4 – The radiation pattern in § 2 is only applicable for one polarization (horizontal or vertical).

NOTE 5 – The radiation pattern included in this Recommendation is only for antennas which are rotationally symmetrical.

NOTE 6 – The average radiation pattern in this Recommendation may be somewhat different from radiation patterns of actual antennas. The purpose of this Recommendation is solely to provide a mathematical model for use in interference assessment for the applications referred to in *considering* c).

NOTE 7 – Radio-relay antennas generally employ linear polarization. Therefore, when the interference from a system employing single circular polarization, such as in the mainbeam-to-mainbeam coupling from space stations, is evaluated, the effective radio-relay antenna gain, *Geff* (ϕ), taking account of polarization advantage, may be estimated by using the following formula within 3 dB of the boresight direction in the main-lobe region (0 < ϕ < ϕ3 dB) instead of the first formula in § 2.1 or 2.2 as demonstrated in Annex 2:



where *G*(ϕ) is the gain according to the first formula in §§ 2.1 and 2.2.

The above formula assumes that the cross-polarized antenna gain for 0° < ϕ < ϕ3 dB is 20 dB lower than *Gmax*. The polarization advantage should not be expected for ϕ > ϕ3 dBor when the radio-relay station is outside the main beam of the antenna of the other service.

The angle ϕ3 dB at which the co‑polarized gain is 3 dB below the maximum gain *Gmax*, can be calculated by replacing *G(*ϕ) with  in the expression for *G*(ϕ) for 0° < ϕ < ϕ*m*:



NOTE 8 – Administrations and other members of ITU-R are encouraged to provide information comparing the average side-lobe levels and the generalized radiation patterns given in this Recommendation with those obtained by radiation pattern measurements on real antennas. This information may assist in the further development of this Recommendation.

NOTE 9 – Administrations and other members of ITU-R are encouraged to examine the feasibility of expanding the application of the model in Annex 1.

Annex 1  
  
Mathematical model of generalized radiation patterns of point-to-point  
fixed-service antennas for use in statistical interference assessment

# 1 Introduction

Recommendation ITU-R F.699 gives the reference radiation patterns of point-to-point fixed service antennas, based on the peak envelope of side-lobe levels. Therefore, the interference assessment using this Recommendation will inevitably lead to overestimation of interference.

On the other hand, the main text of this Recommendation gives a mathematical model for average radiation patterns of point-to-point fixed service antennas, representing average side-lobe levels. However, this can be applied only in the case of multiple interference entries or time-varying interference entries.

A mathematical model is required for generalized radiation patterns of antennas for use only in spatial statistical analysis such as deriving the probability distribution function (pdf) of interference from a few GSO satellite systems into a large number of interfered with fixed service systems or stations.

# 2 Antennas with *D*/λ greater than 100

The reference radiation pattern of antennas with *D*/λ greater than 100 representing peak envelope side-lobe levels is given by *recommends* 2.1 of Recommendation ITU-R F.699. According to *recommends* 2.1 of this Recommendation, the average side-lobe level is 3 dB below the peak envelope side-lobe level. It seems reasonable to assume that the actual side-lobe levels vary sinusoidally. Therefore, the actual radiation pattern will be expressed as follows:

*G*(ϕ)  max [*Ga*(ϕ), *Gb*(ϕ)] for 0 ≤ ϕ < ϕ*r* (1a)

 *G*(ϕ)  32 – 25 log ϕ *F*(ϕ)for ϕ*r*≤ ϕ < 48o (1b)

*G*(ϕ)–10  *F*(ϕ) for 48o ≤ ϕ ≤ 180o (1c)

where:

 (1d)

*Gb*(ϕ)*G*1 + *F*(ϕ) (1e)

*G*1  2  15 log (*D*/λ) dB (2a)

ϕ*r*  15.85  degrees (2b)

*F*(ϕ)10 log  dB (2c)

where ϕ*r* is assumed to correspond to the off-axis angle of the peak of the first side-lobe and the phase at ϕ  ϕ*r* is assumed to be 1.5π. It should be noted that the argument of sin function in equation (2c) is expressed in radians and that the value of *F*(ϕ) is nearly zero or negative. *F*(ϕ)  0 corresponds to side-lobe peaks. The parameter 0.1 is introduced in equation (2c) in order to avoid the situation that *F*(ϕ) falls below –10 dB.

# 3 Antennas with *D*/λ equal to or smaller than 100

In the case of antennas with *D*/λ equal to or smaller than 100, it will be assumed that side-lobe peak levels are 3 dB higher than the average side-lobe level given in the main text of this Recommendation.

Thus, the following pattern is provisionally presented as a generalized radiation pattern of the antenna with *D*/λ equal to or smaller than 100:

*G*(ϕ)  max [*Ga*(ϕ), *Gb*(ϕ)] for 0 ≤ ϕ < ϕ*r* (3a)

 *G*(ϕ)  42 – 5 log (*D*/λ) – 25 log ϕ *F*(ϕ)for ϕ*r*≤ ϕ < 48o (3b)

*G*(ϕ)–5 log (*D*/λ)  *F*(ϕ) for 48o ≤ ϕ ≤ 180o (3c)

where:

 (3d)

*Gb*(ϕ)*G*1 + *F*(ϕ) (3e)

*G*1  2  15 log (*D*/λ) dB (4a)

ϕ*r*  39.8 degrees (4b)

*F*(ϕ)10 log  dB (4c)

Again, it should be noted that the argument of sin function in equation (4c) is expressed in radians and that the value of *F*(ϕ) is nearly zero or negative and *F*(ϕ)  0 corresponds to side-lobe peaks. The reason for introducing the parameter 0.1 in equation (4c) is the same as that for equation (2c).

# 4 Conclusion

Equations (1a) to (1e) (together with (2a) to (2c)) and (3a) to (3e) (together with (4a) to (4c)) are provisionally presented as mathematical models of generalized radiation patterns of point-to-point fixed service antennas for use only in spatial statistical interference assessment.

Annex 2  
  
Derivation of *Geff* (ϕ) in Note 7 regarding polarization advantage  
between linear-polarized and circular-polarized systems

# 1 Introduction

Radio-relay antennas generally employ linear polarization. Therefore, when the interference from a system employing single circular polarization comes into the radio-relay antennas, it is important to evaluate the circular to linear polarization loss, or polarization advantage between linear‑polarized and circular-polarized systems. In the ideal case, the circular to linear polarization loss will be 3 dB. Practical systems will achieve somewhat less polarization discrimination than in the ideal situation.

This Annex discusses the derivation of a circular to linear polarization loss in practical cases.

# 2 Equation for polarization loss for non-ideal antennas

The polarization loss for non-ideal antennas is generally given by the following:



where:

*Lp*: polarization loss

*rw*: voltage axial ratio of the radio wave

*ra*: voltage axial ratio of the antenna

Δτ: angle between the tilt angle of the antenna polarization ellipse and the tilt angle of the incident wave polarization ellipse, both referred to horizontal at the Earth’s surface. For the purposes of this analysis, it is assumed that Δτ = 0, which is the most conservative case.

For a circularly polarized antenna, the voltage axial ratio is usually specified in decibels. These terms are related by the relationship: . For a linearly polarized antenna, the decibel axial ratio is equivalent in magnitude to the antenna cross-polarization isolation as in the following relationship: .

Figure 1 below shows a plot of polarization loss, *Lp*, versus cross-polarization isolation (XPI) for three values of circular polarization axial ratio, *R*. This plot is independent of frequency.

Figure 1

Polarization loss vs. XPI for various values of *R*



The appropriate value of *Lp* will depend on the characteristics of circularly and linearly polarized antennas through the frequency range from 1 to 70 GHz.

# 3 Examples of the XPI data

Examples of the XPI data of fixed service antennas from two administrations are shown in Tables 1 and 2. Table 1 contains a summary of information from one administration’s licensing database for a range of frequency bands from around 1 GHz up to 40 GHz; and Table 2 shows another XPI data based on different antenna types used in another administration for frequency bands from about 6 GHz up to 22 GHz.

TABLE 1

Example of the XPI data in one administration

| Band  (GHz) | Number of antenna records | 5th percentile XPI (dB) | 10th percentile XPI (dB) | Median XPI  (dB) |
| --- | --- | --- | --- | --- |
| 0.953-1.525 | 484 | 12 | 20 | 30 |
| 1.7-2.7 | 698 | 20 | 20 | 30 |
| 3.4-5.0 | 280 | 15 | 20 | 30 |
| 5.85-7.125 | 532 | 20 | 28 | 30 |

TABLE 1 (*end*)

| Band  (GHz) | Number of antenna records | 5th percentile XPI (dB) | 10th percentile XPI (dB) | Median XPI  (dB) |
| --- | --- | --- | --- | --- |
| 7.125-7.725 | 403 | 24 | 28 | 30 |
| 7.725-8.5 | 213 | 30 | 30 | 30 |
| 10.5-10.68 | 151 | 28 | 30 | 30 |
| 10.7-11.7 | 202 | 20 | 25 | 30 |
| 12.7-13.25 | 209 | 25 | 25 | 30 |
| 14.5-15.35 | 172 | 28 | 30 | 30 |
| 17.7-19.7 | 181 | 27 | 30 | 30 |
| 21.2-23.6 | 164 | 25 | 28 | 30 |
| 24.25-25.25 | 8 | 30 | 30 | 32 |
| 24.35-28.35 | 4 | 30 | 30 | 32 |
| 28.6-40.0 | 30 | 23 | 26 | 30 |

TABLE 2

Example of the XPI data in another administration

|  |  |  |  |  |
| --- | --- | --- | --- | --- |
| Band  (GHz) | Number of antenna types | Number of deployed antennas | 10th percentile XPI (dB) | Average XPI  (dB) |
| 5.925-7.75 | 11 | 600 | 25 | 29 |
| 10.7-15.23 | 27 | 5 700 | 32 | 35 |
| 17.85-23.2 | 13 | 2 806 | 26 | 28 |

According to this data, an assumption of a minimum XPI of 20 dB would seem to be appropriate at the frequencies up to 40 GHz.

Although antenna performance data above 40 GHz is not available, the trend is towards equal or better cross-polarization performance as frequency increases. Therefore, pending the availability of more specific data for linearly polarized antennas in higher bands and consistent with *recommends*2, it can tentatively be concluded that a minimum XPI of 20 dB may also be used between 40 GHz and 70 GHz.

# 4 Conclusion

Taking into account Tables 1 and 2, an XPI of 20 dB of radio-relay antenna is appropriate. Taking into account Fig. 1, for an XPI of 20 dB and a tentative interfering antenna maximum circular polarization axial ratio (R) of 1.5 dB, which is applicable around the boresight direction of space stations antenna not practicing frequency reuse by orthogonal polarization operated at around 2 to 30 GHz frequency bands, the polarization loss would be 1.7 dB. This value would be applicable only within the antenna 3 dB beamwidth of radio-relay antenna and around the boresight direction of space stations antenna and should be applicable between 1 and 70 GHz.

1. \* This Recommendation should be brought to the attention of Radiocommunication Study Groups 4 and 7. [↑](#footnote-ref-1)