

Economic Period of Provisioning

Planning of Fiber Optics Cable

Solution of Case Study

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1. **Calculation of circuits required between transit exchanges**

From Table 1 providing the trunks needed for the next three years, we get:

$$877 + 888 = 1765 \text{ trunks.}$$

2. **Calculation of demand growth**

The annual demand growth for PCM systems is found:

- annual demand growth for circuits:

$$1765/3 = 588,3 \text{ circuits/year}$$

- annual demand growth for transmission systems of 1920 channels:

$$\lambda = 588,3/1920 = 0.3064 \text{ system/year}$$

3. **Calculation of cable parameters**

- Calculation of *pvf* μ_c

$$\mu_c = 1 + \frac{I}{(1+i)^T - 1} + \frac{u}{i}$$

For $i = 0.1$, $T = 18$ years, and $u = 0.035$, we get:

$$\mu_c = 1 + \frac{I}{1.1^{18} - 1} + \frac{0.035}{0.1} = 1.57$$

- Calculation of capital basic cost. Let

$$\hat{\mu}_c = 1 + \frac{I}{(1+i)^T - 1} = 1.22$$

be the *pvf*, taking into account only the replacement of cable. Then, we have

$$a = \text{purchasing cost} \times \mu_c + (\text{taxes} + \text{digging cost} + \text{placement of cable}) \times \mu_c$$
$$a = 600 \cdot 1.57 + (600 \cdot 0.2 + 750 + 80) \cdot 1.22 = 2100 \text{ MU / km}$$

- Calculation of capital incremental cost b

$$b = \text{purchasing cost} \times \mu_c + (\text{taxes} + \text{jointing and testing}) \times \mu_c$$

$$b = 720 \cdot 1.57 + (720 \cdot 0.2 + 15) \cdot 1.22 = 1324 \text{ MU / pair / km}$$

4. **Economic period of provisioning**

The provisioning period is given by

$$t = \frac{1}{r} \ln(1 + p + 2p), \quad p = ar / (b\lambda) = 0.492$$

$$t = \ln(1 + 0.492 + \sqrt{2 \cdot 0.492}) = 9.57 \text{ years}$$

5. **Optimal size of cable**

$$s = \lambda t = 9.57 \cdot 0.3064 = 2.94 = 3 \text{ pairs}$$

Thus, the optimal size of cable should be 6 fibers.

6. **Calculation of present worth of expenditure to implement the fiber optics Link**

$$PW = \frac{a + bs}{1 - e^{-rs/\lambda}} \lambda = \frac{2100 + 1324 \cdot 3}{1 - e^{-0.095 \cdot 3 / 0.3064}} 170 = 1,704,750 \text{ MU}$$

7. **Calculation of annual charges (AC)**

$$(AC) = PW \cdot i = 1704750 \cdot 0.1 = 170.475 \text{ MU / year}$$

8. **Present worth of expenditures for double size cable**

$$PW_{2s} = \frac{a + b2s}{1 - e^{-r2s/\lambda}} \lambda = \frac{2100 + 2 \cdot 1324 \cdot 3}{1 - e^{-0.095 \cdot 6 / 0.3064}} \cdot 170 = 2,022,179 \text{ MU}$$

Percentage variation with respect to minimum cost variation

$$= \frac{2022179 - 1704750}{1704750} \cdot 100 = 18.6\%$$